

IOWA STATE UNIVERSITY

# Modeling the Operations of Electric Autonomous Taxis in New York City

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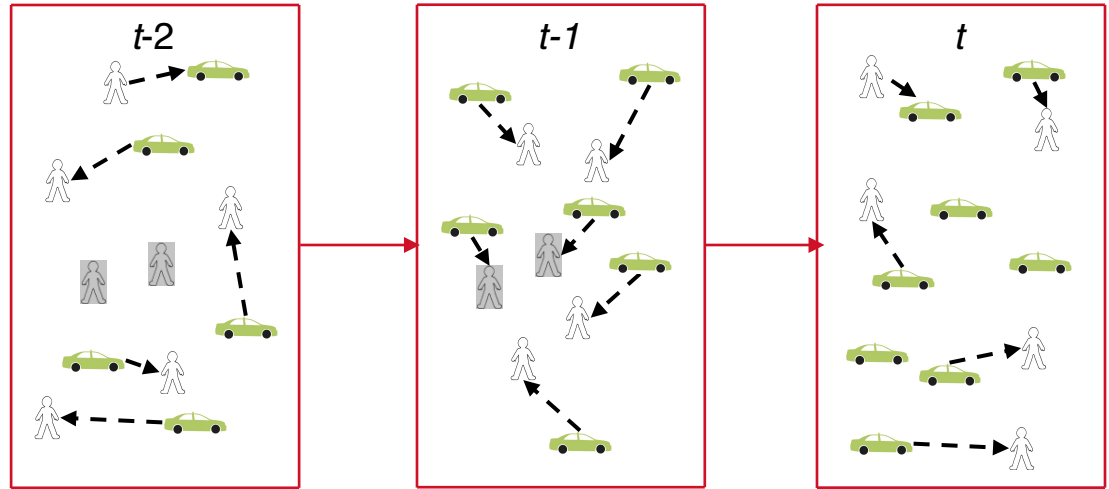
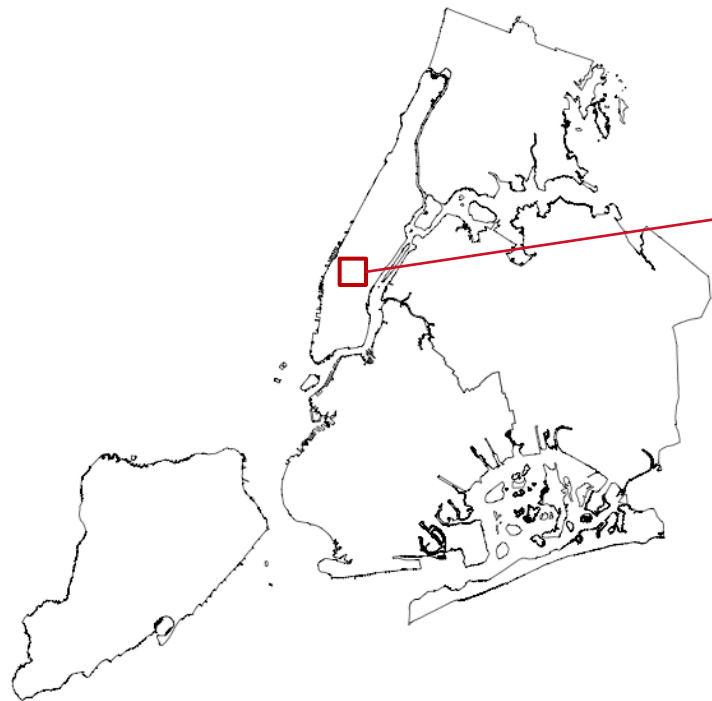
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# Why Electric Autonomous Taxis?

	Conventional taxis	Ride-hailing	Electric autonomous vehicles (EAV)
Energy source	<ul style="list-style-type: none"> <li>gasoline</li> <li>some electric</li> </ul>	<ul style="list-style-type: none"> <li>gasoline</li> <li>some electric</li> </ul>	<ul style="list-style-type: none"> <li>electric</li> </ul>
Search for customers	<ul style="list-style-type: none"> <li>cruising</li> <li>by chance</li> </ul>	<ul style="list-style-type: none"> <li>cruising + waiting</li> <li>drivers compete</li> </ul>	<ul style="list-style-type: none"> <li>relocating + waiting</li> <li>collaborative</li> </ul>
Customers' delay	<ul style="list-style-type: none"> <li>unknown to taxis</li> </ul>	<ul style="list-style-type: none"> <li>drivers do not care</li> </ul>	<ul style="list-style-type: none"> <li>optimal dispatch</li> <li>reduce delay</li> </ul>
Trip distance	<ul style="list-style-type: none"> <li>unknown to taxis</li> </ul>	<ul style="list-style-type: none"> <li>unknown to taxis</li> </ul>	<ul style="list-style-type: none"> <li>taxis w/o sufficient range are not assigned</li> </ul>

# Model EAV Taxi Operations



Model operations based on status of both requests and taxis, over time, area by area



Requests

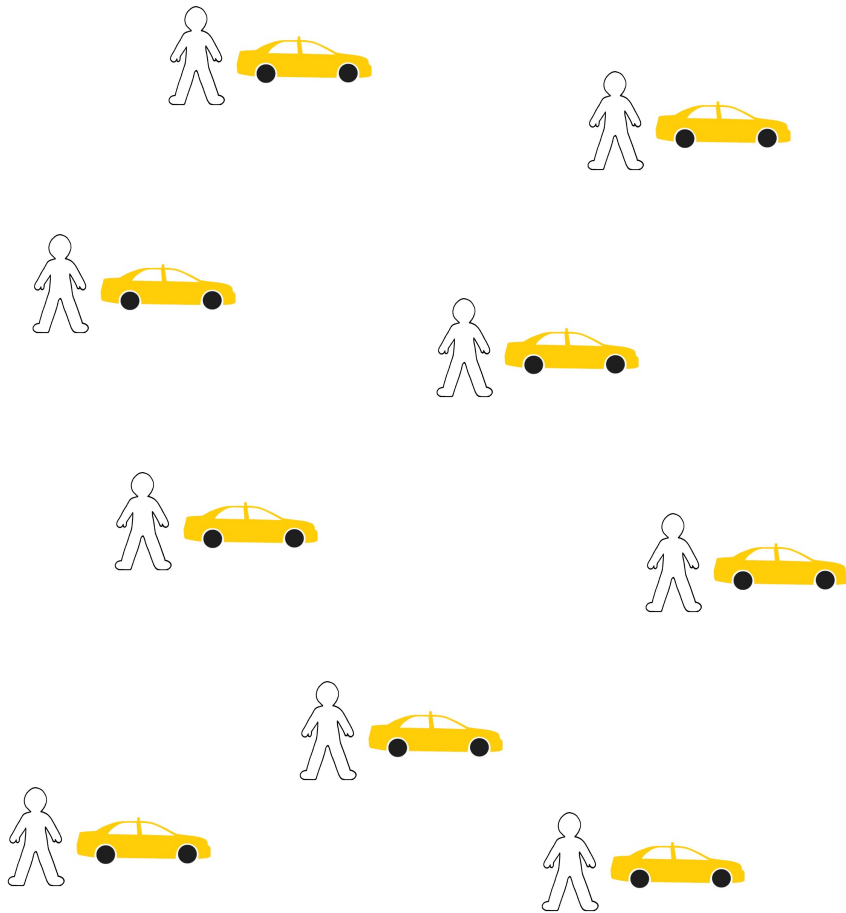
- request time
- location
- wait time



EAV taxis

- location
- SOC

# Taxi Trip Data in NYC

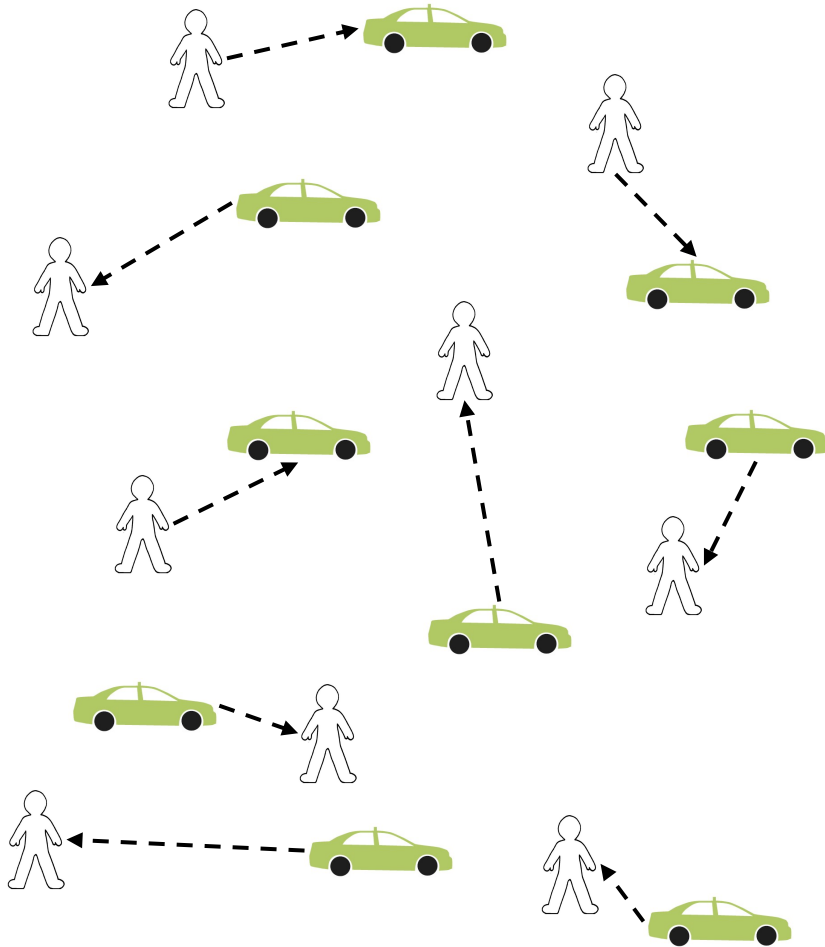


- ❑ Data fields
  - taxi ID
  - pick-up GPS
  - pick-up timestamp
  - drop-off GPS
  - drop-off timestamp
  - occupied trip distance

- ❑ Estimate empty trip dist. by  
 $\text{trip dist.} = 1.4413 \times \text{straight-line dist.} + 0.1383$  (unit: mi)

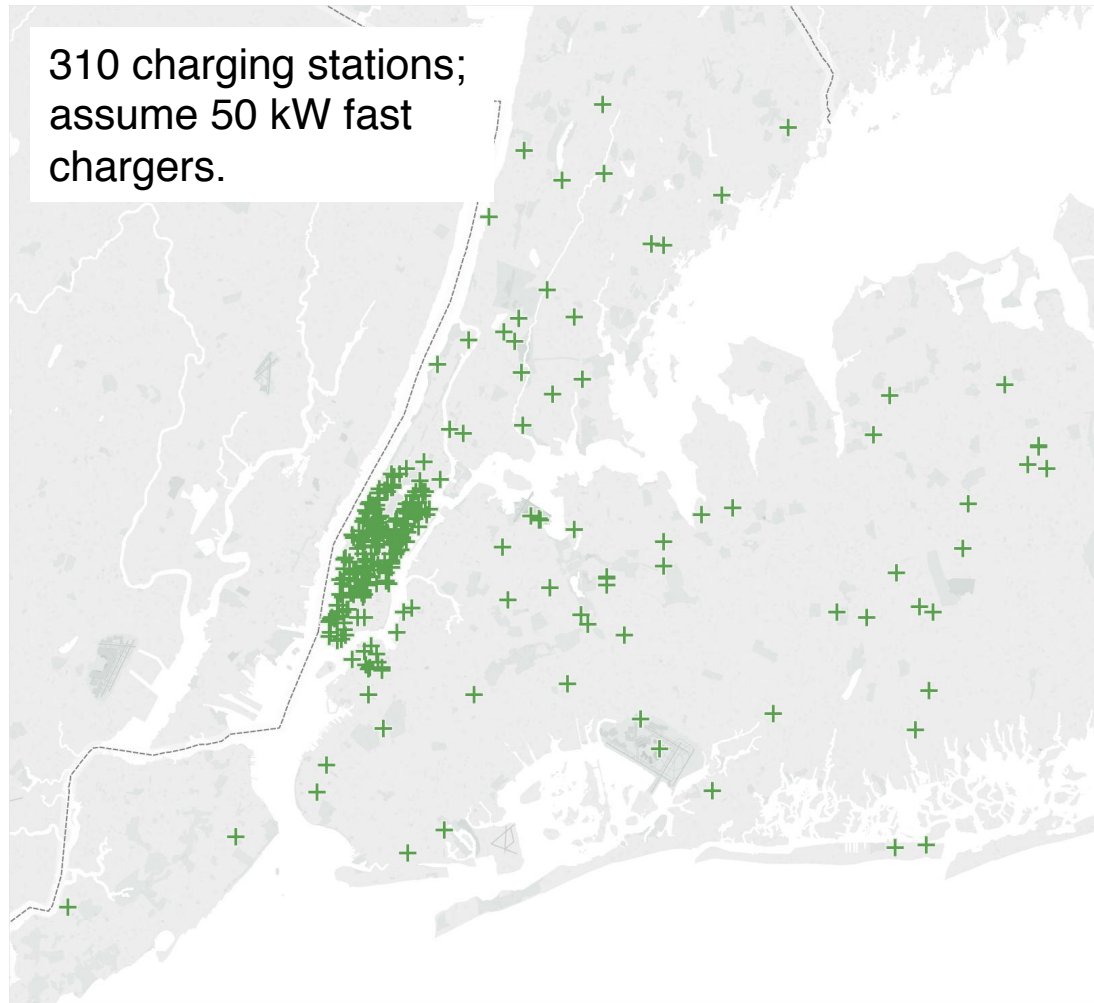
- ❑ Extract data of 500 taxis & the corresponding requests

# Assumptions for Simulation



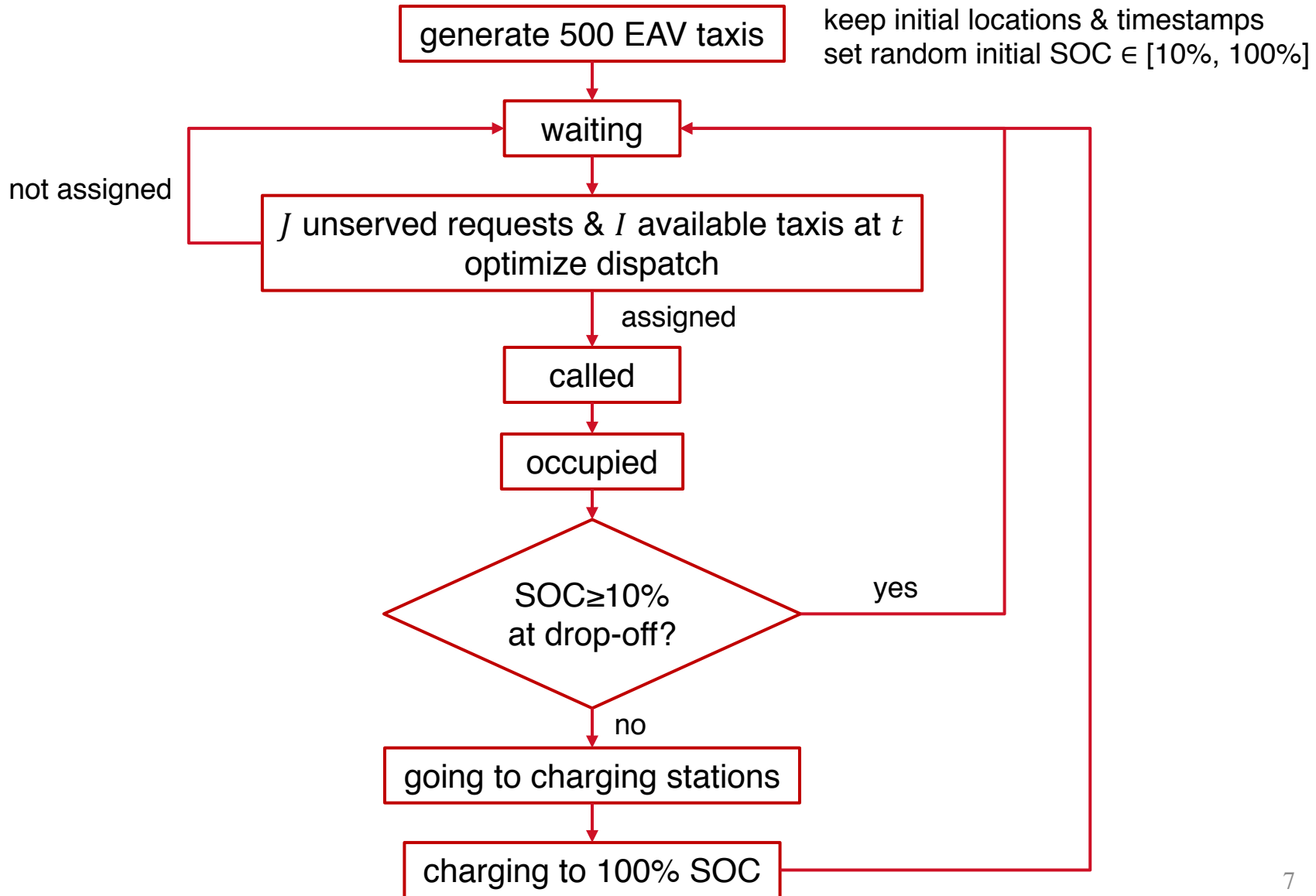
- ❑ Requests of customers
  - location: pick-up GPS
  - time: pick-up timestamp
  - dist.: occupied trip dist.
- ❑ EAV taxis
  - location: drop-off GPS
  - time: drop-off timestamp
  - dist.: estimated trip dist.

# Charging Stations in NYC



Source: US DOE

# Simulation Process



# Decision Variables

$I$  available taxis and  $J$  unserved requests at  $t$

Define binary decision variables

$$x_{i,j}$$

$i$ : index of an available taxi,  $i \in I$

$j$ : index of an unserved request,  $j \in J$


$x_{i,j} = 1$ : taxi  $i$  picks up request  $j$


$x_{i,j} = 0$ : taxi  $i$  does not pick up request  $j$



# Objective Function

minimize 
$$\sum_{i=1}^I \sum_{j=1}^J D_{i,j}^{(1)} x_{i,j} + \sum_{j=1}^J D_j^{(2)} \left(1 - \sum_{i=1}^I x_{i,j}\right)$$

 total costs of the requests that can be served

 total costs of the requests that cannot be served

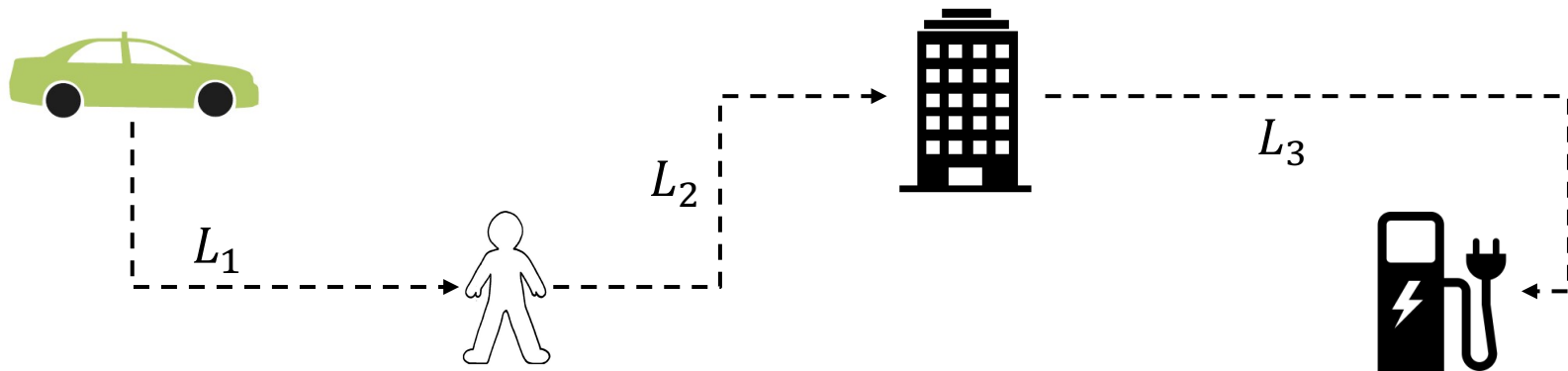
$D_{i,j}^{(1)}$ : cost matrix (1) = time that has been delayed + time for pick-up

$D_j^{(2)}$ : cost matrix (2) = time that has been delayed + avg. wait time

  
differs by area

# Constraints (1): Sufficient EV Range

- calculate the distance matrix  $L_{I \times J} = L_1 + L_2 + L_3$



- if  $L_{i,j} >$  the taxi's remaining range,

$$x_{i,j} = 0$$

## Constraints (2)

- Each taxi will server at most one customer

$$\sum_{j=1}^J x_{i,j} \leq 1, \forall I$$

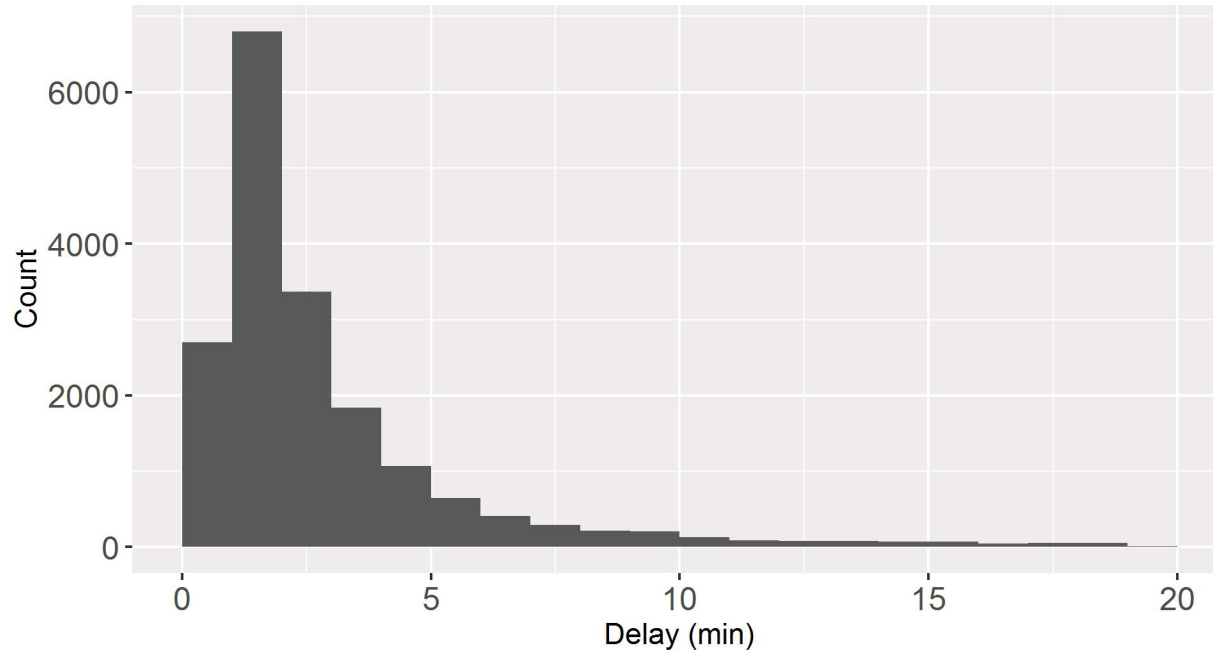
- Each customer will be served by at most one taxi

$$\sum_{i=1}^I x_{i,j} \leq 1, \forall J$$

# Solver

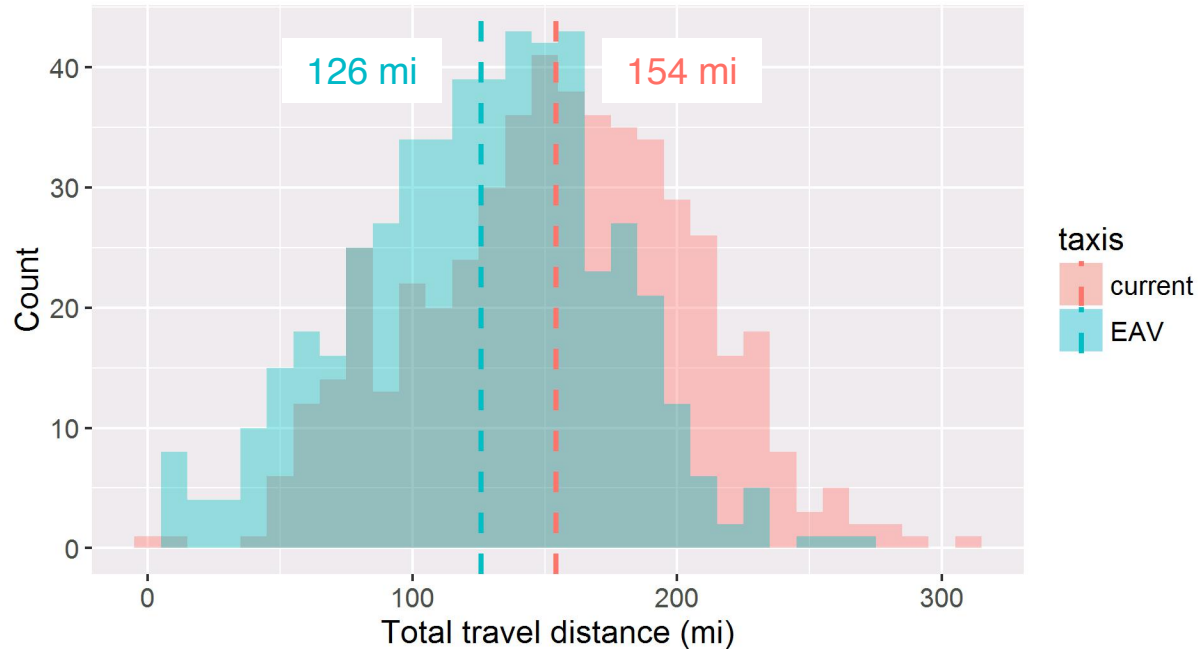
- ❑ Gurobi 7.5.1
- ❑ integer linear programming (ILP)
- ❑ 1440 time intervals
- ❑ CPU Intel E5-1620 3.70GHz, RAM 16GB
- ❑ ~40 minutes

# Customer Wait Time Distribution



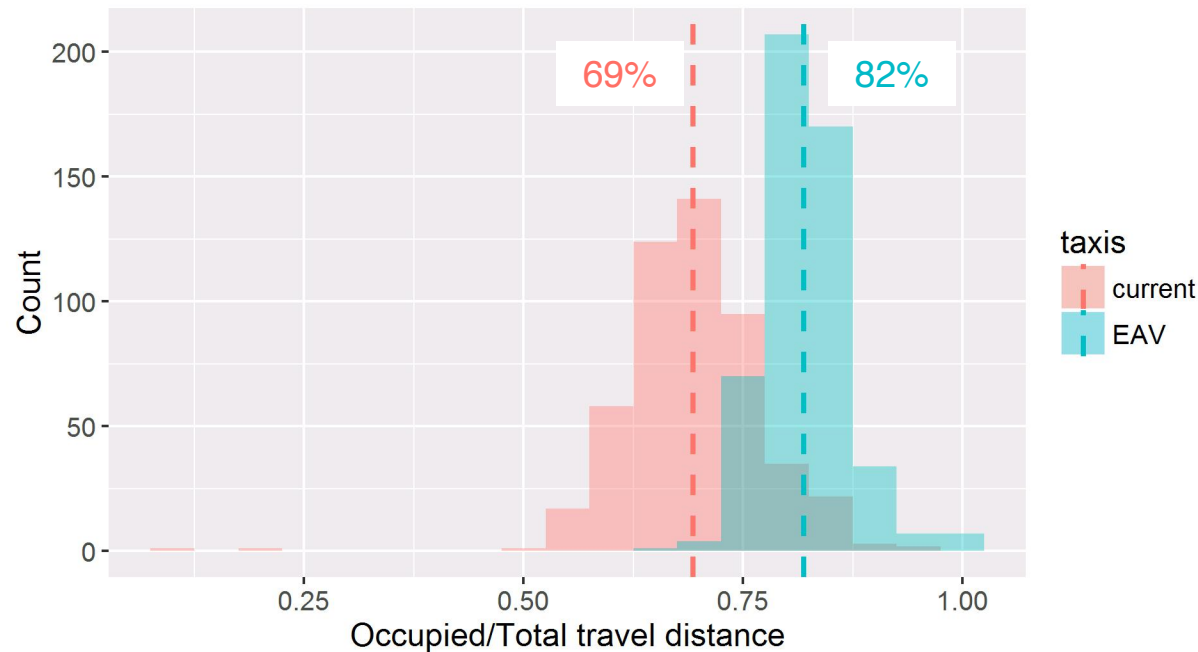
- Only **0.5%** of requests are not served
- Average wait time is **4.7** minutes
- 95% of requests are served within **11** minutes

# Total Travel Distance of Taxis



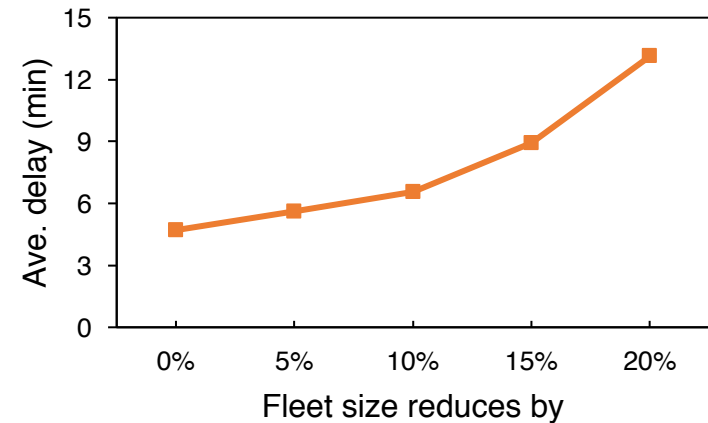
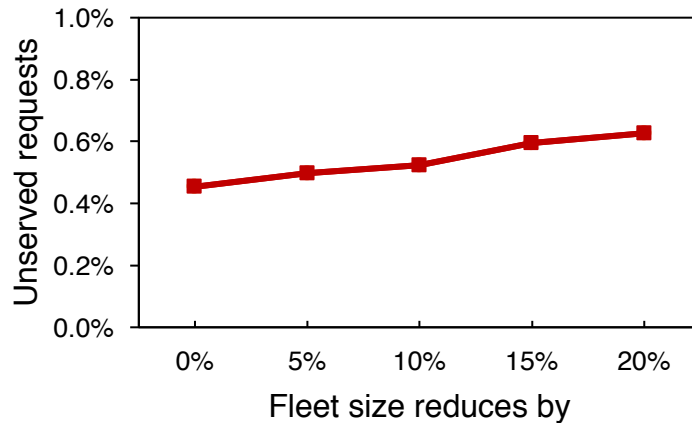
- Average travel distance reduces by **18%**

# Ratio of Occupied/Total Travel Distance



- EAV taxi system reduces empty trip distance from **49 mi** to **23 mi**
- Average ratio of occupied distance increases from **69%** to **82%**

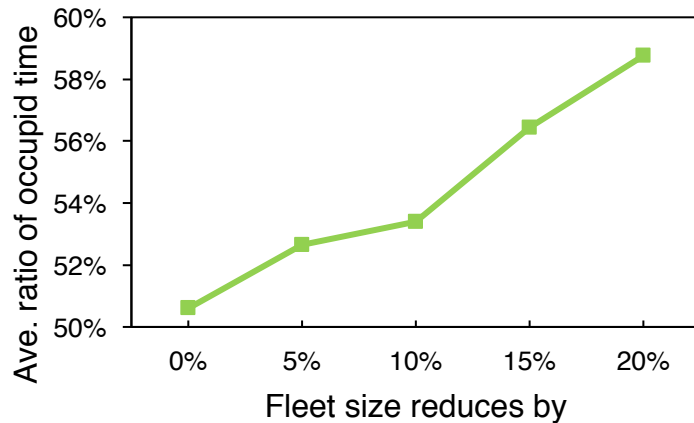
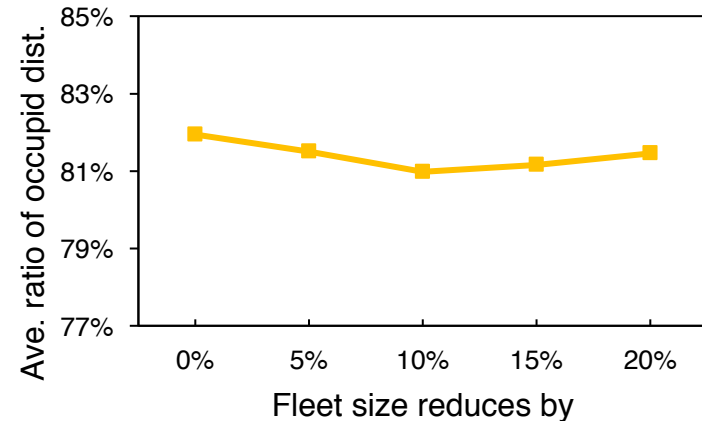
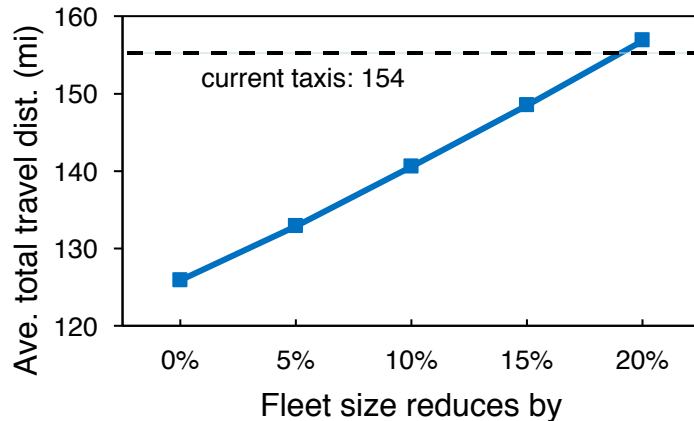
# Implications of Fleet Size



- Reduces fleet size by **5%~20%**
- Unservd requests remain at **0.5%~0.6%**
- Average delay is **within 9 minutes** when fleet size reduces by **≤15%**
- Average delay increases more significantly at 20% reduction

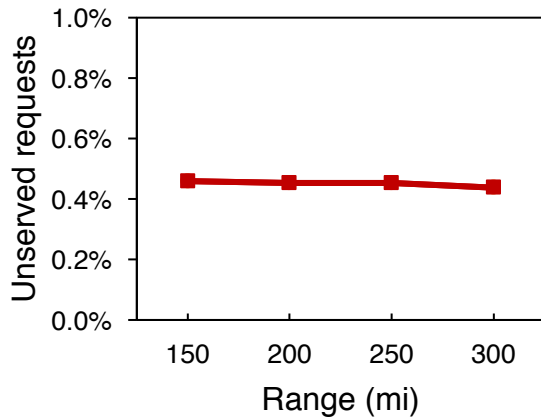


# Implications of Fleet Size

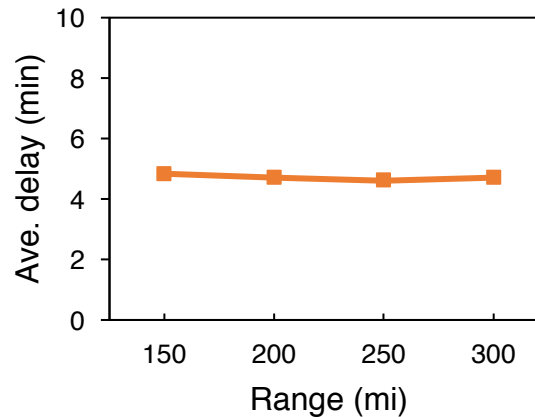


- With smaller fleet size, EAV taxis become busier
  - travel distance & ratio of occupied time increase almost linearly
- Efficiency of current taxi system  $\approx$  EAV taxis with **80%** of fleet size
- Ratio of occupied distance remains stable at **81%~82%**

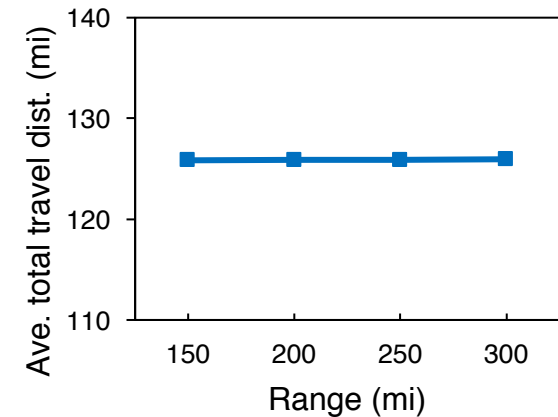
# Implications of Electric Range



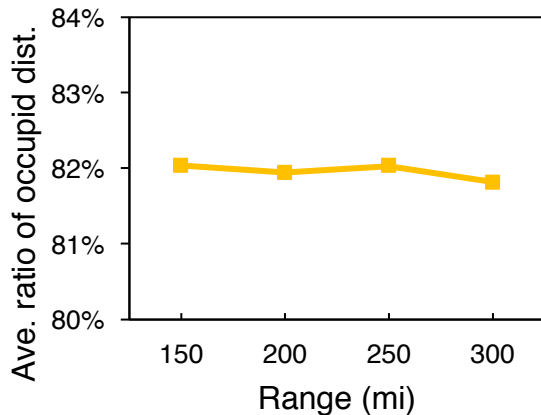
unserved requests: 0.5%



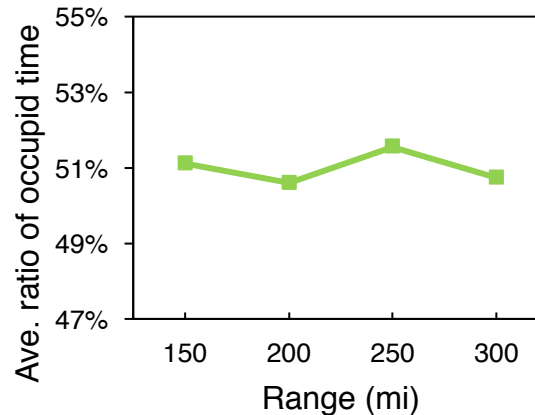
avg. delay: 4.6~4.8 min



avg. total travel dist.: 126 mi



avg. ratio of occupied dist.: 82%



avg. ratio of occupied time: 51%~52%

- Range does not have considerable implications on request delays nor efficiency of EAV taxi systems

# Summary

- ❑ EAV taxis improves efficiency of taxi systems
  - less empty trips
  - less energy consumption
- ❑ EAV taxis has potential to reduce fleet size, while keep wait time at an acceptable level
  - average delay is within 9 min when the fleet size is reduced by 15%

# Thank you

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